A fluorescence microscopy image showing a network of cells. The nuclei are stained blue, and the cytoplasm and cell membranes are stained green. The cells are interconnected, forming a complex, web-like structure. The background is dark, making the fluorescent structures stand out.

# Optical fluorescence: spectroscopy and microscopy

Bill Rose

# Outline

## 1. Basic concepts and definitions

Fluorescence, phosphorescence, transmittance, absorbance, lifetime

## 2. Spectroscopy tools

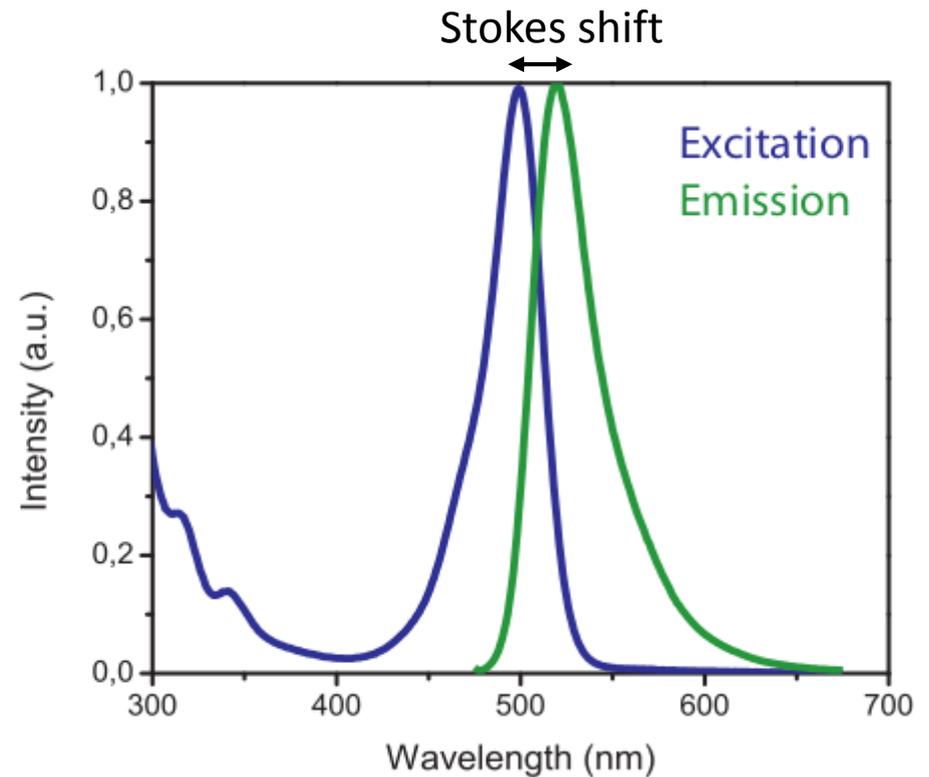
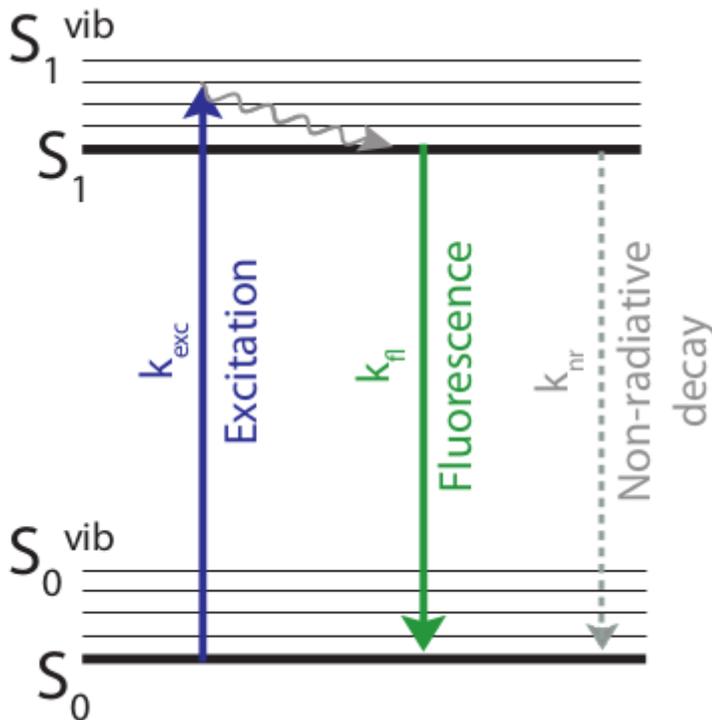
## 3. Fluorescence Imaging techniques

## 4. Applications

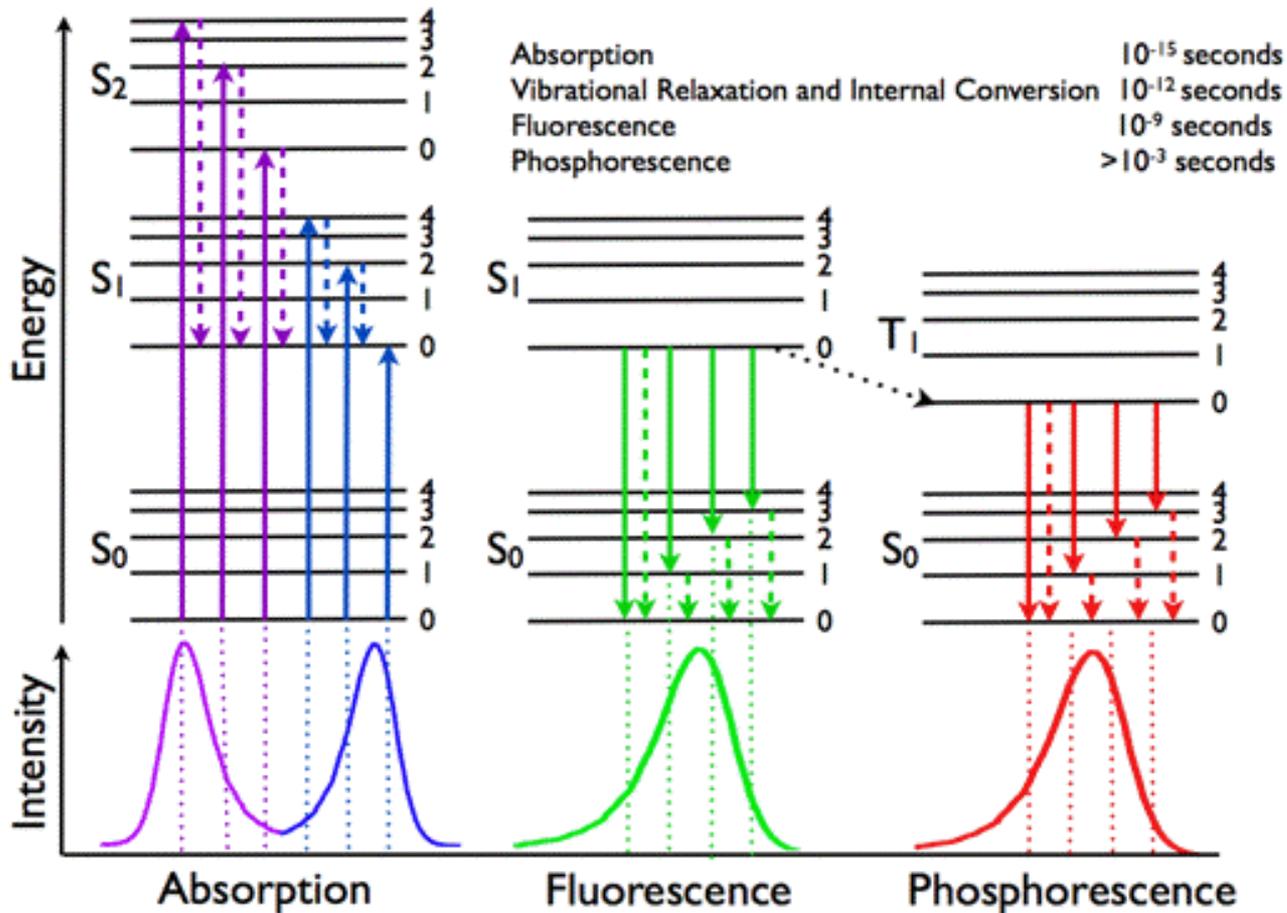
# Fluorescence

Emission of photon during atomic transition to lower-energy state

$$E_\gamma = \frac{hc}{\lambda}, k = \frac{2\pi}{\lambda}$$



# Phosphorescence



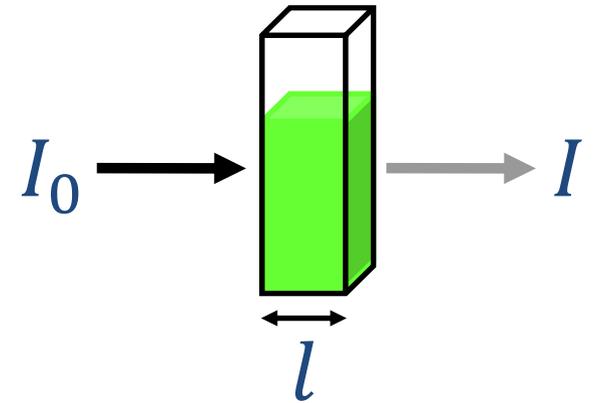
Transition from excited triplet state to singlet ground state

Much slower due to 'forbidden' spin transition

# Transmittance ( $T$ ) and Absorbance ( $A$ )

Transmittance:  $T = \frac{I}{I_0} = 10^{-A}$

Absorbance:  $A = \varepsilon(\lambda) * cl$



$\varepsilon(\lambda)$ : molar attenuation constant

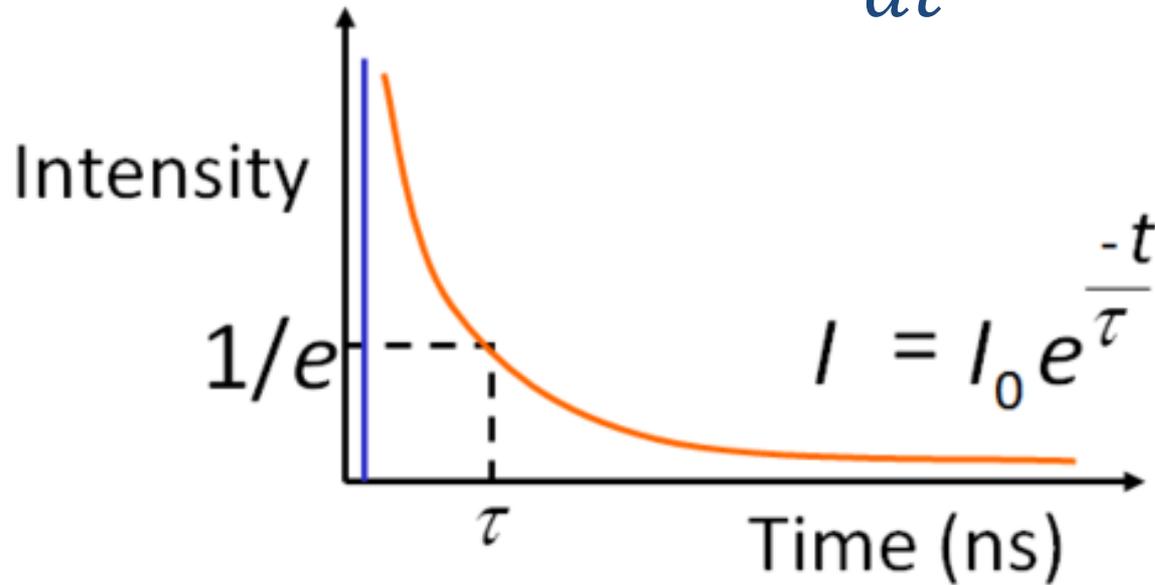
$c$ : amount concentration

$l$ : path length

# Lifetime ( $\tau$ )

$$\frac{dS_1}{dt} = -\frac{S_1}{\tau} \Rightarrow S_1(t) = S_1(0) * e^{-t/\tau}$$

$$I \propto \frac{dS_1}{dt} \propto S_1$$



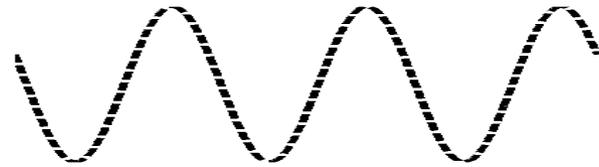
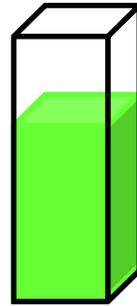
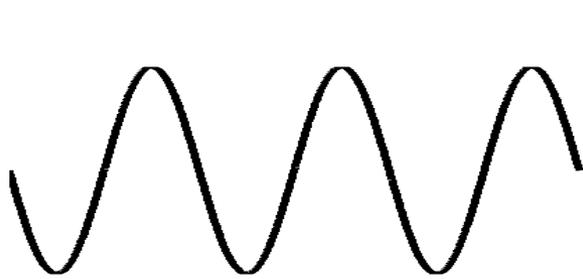
Fluorescence  
lifetime:

$$\tau \sim ns$$

Phosphorescence  
lifetime:

$$\tau \sim ms$$

# Frequency-domain Lifetime Measurement



$$E(t) = E_0 + E_\omega \cos(\omega t + \varphi_e)$$

$$F(t) = F_0 + F_\omega \cos(\omega t + \varphi_e - \varphi)$$

$$M = \frac{F_\omega / F_0}{E_\omega / E_0} = \frac{1}{\sqrt{1 + (\omega\tau)^2}}, \quad \tan(\varphi) = \omega\tau$$

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Monochromator, diffraction grating, prism, spectrophotometer, fluorophores

## 3. Fluorescence Imaging techniques

## 4. Applications

# Monochromator

Czerny-Turner  
Monochromator:

A: Incoming light

B: Entrance slit

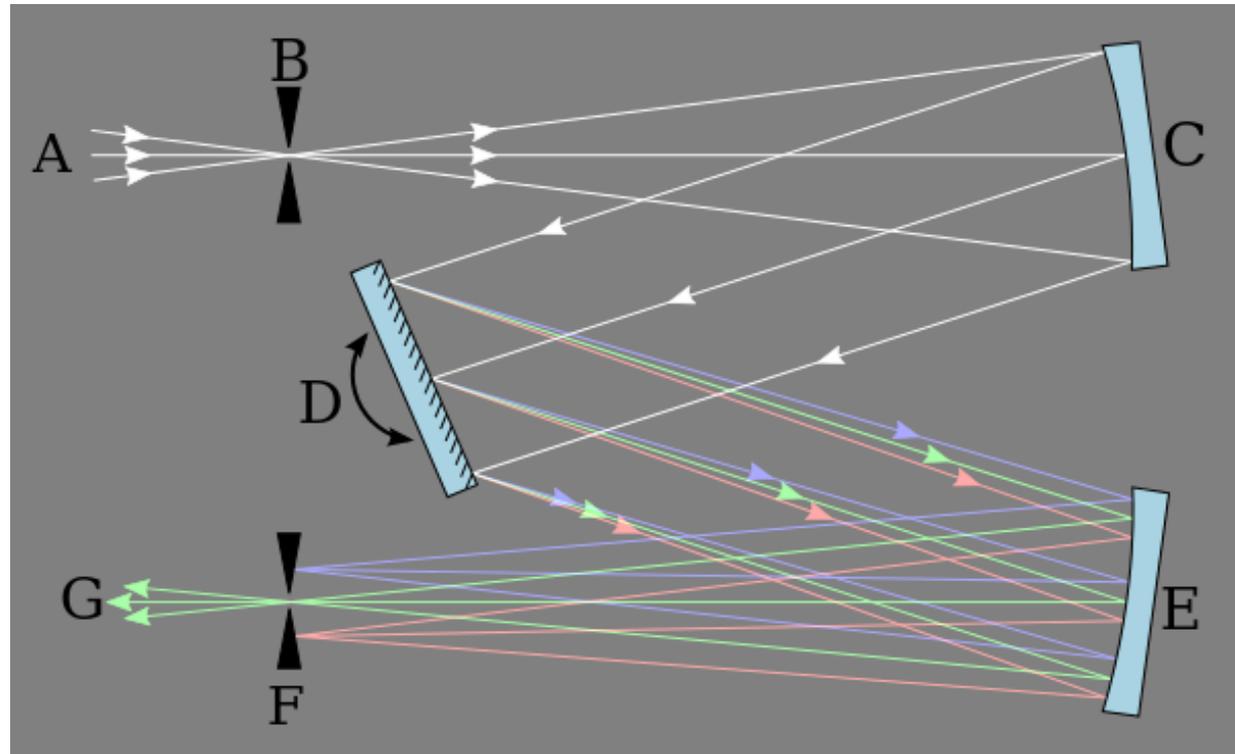
C: Collimating mirror

D: Diffraction grating /  
Refracting prism

E: Refocusing mirror

F: Exit slit

G: Outgoing light



[https://en.wikipedia.org/wiki/Monochromator#/media/File:Czerny-Turner\\_Monochromator.svg](https://en.wikipedia.org/wiki/Monochromator#/media/File:Czerny-Turner_Monochromator.svg)

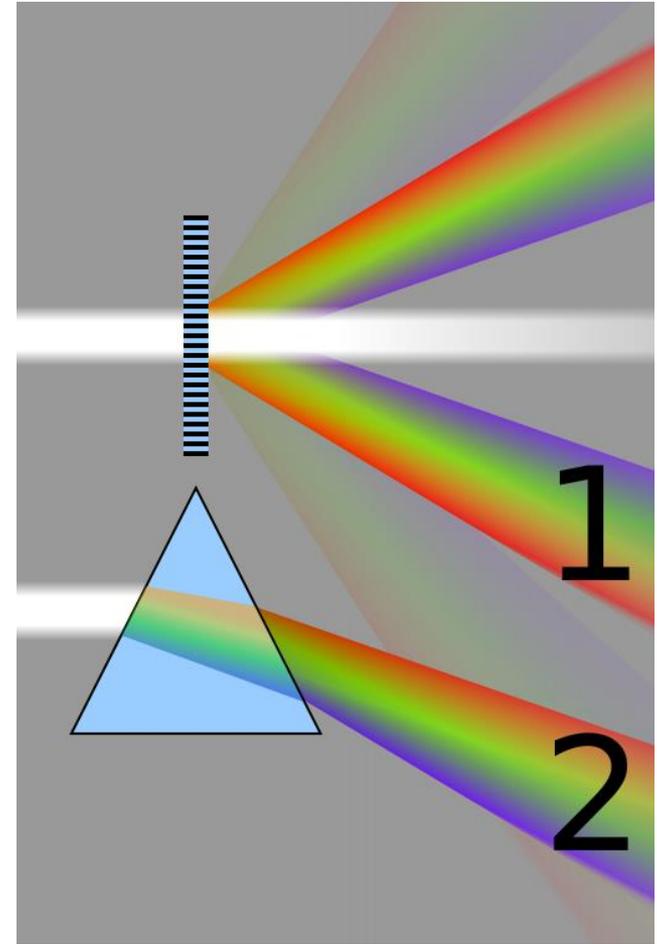
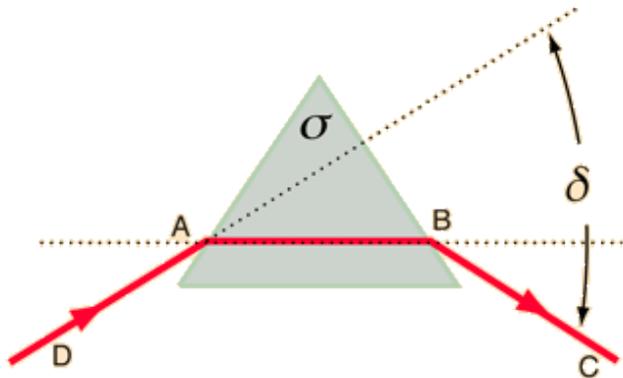
# Light splitting

(1) Diffraction grating:

$$\theta = \sin^{-1} \left( \frac{\lambda}{d} - \sin \theta_i \right)$$

(2) Prism:

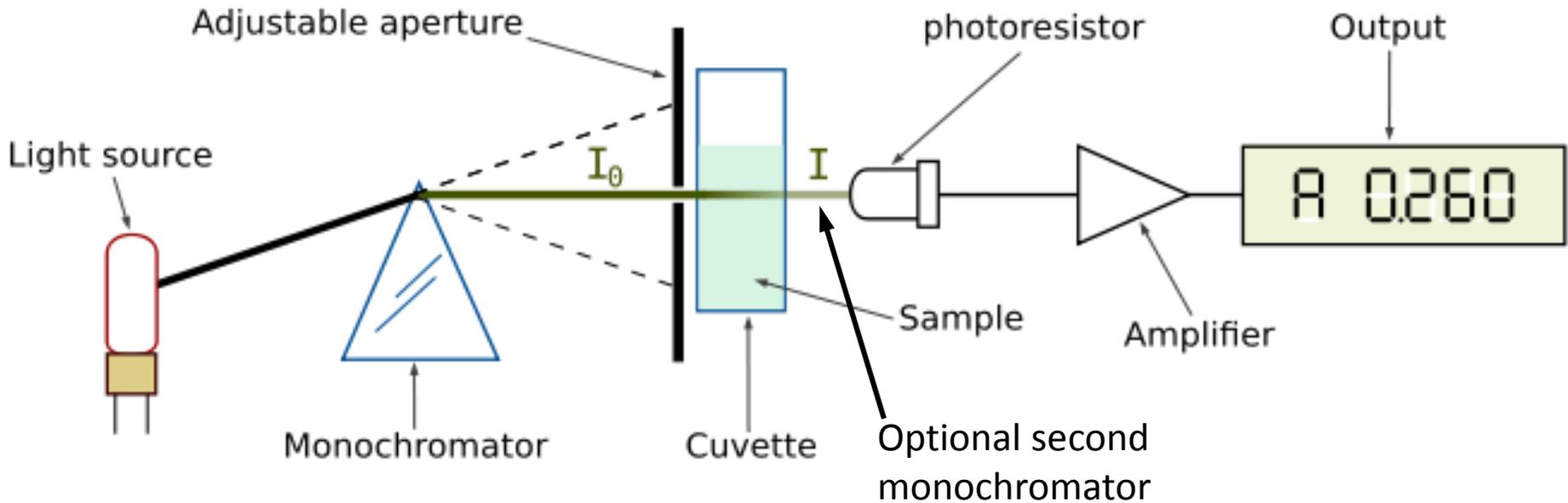
$$\delta = 2 \sin^{-1} \left( \frac{n_p(\lambda)}{n_0} \sin \frac{\sigma}{2} \right) - \sigma$$



[https://en.wikipedia.org/wiki/Diffraction\\_grating#/media/File:Comparison\\_refraction\\_diffraction\\_spectra.svg](https://en.wikipedia.org/wiki/Diffraction_grating#/media/File:Comparison_refraction_diffraction_spectra.svg)

# Spectrophotometer

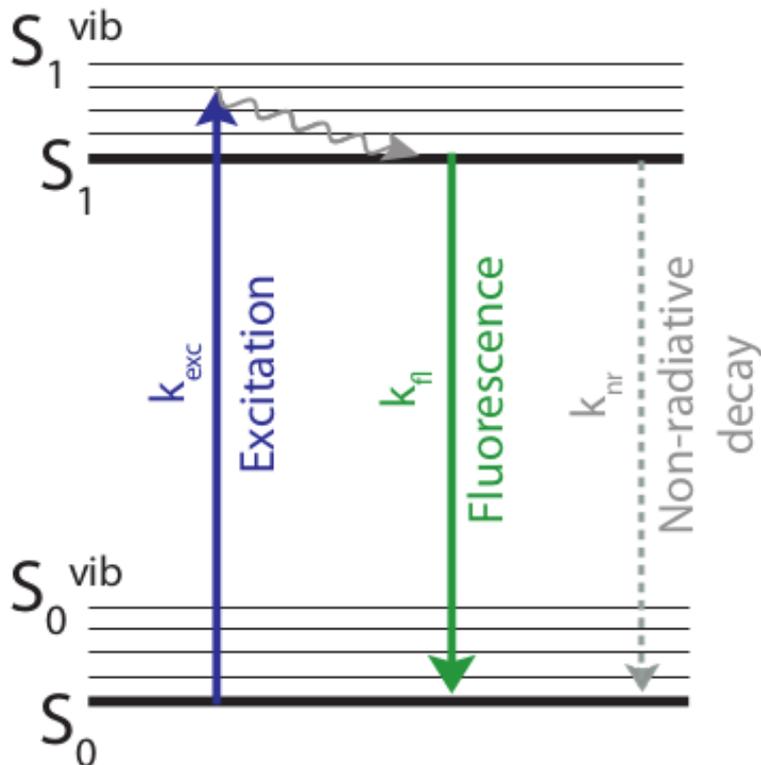
System for measuring absorption (and emission) spectra



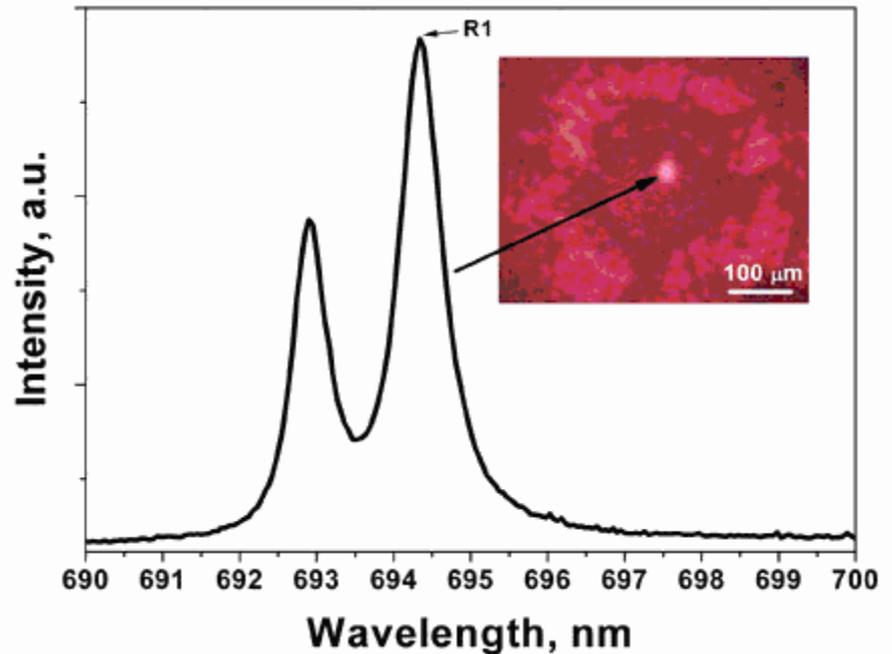
# Fluorescence spectroscopy

- Can be used to measure energy differences between excited and ground states
- Can resolve fine structure

$$E_{\gamma} = \frac{hc}{\lambda}$$

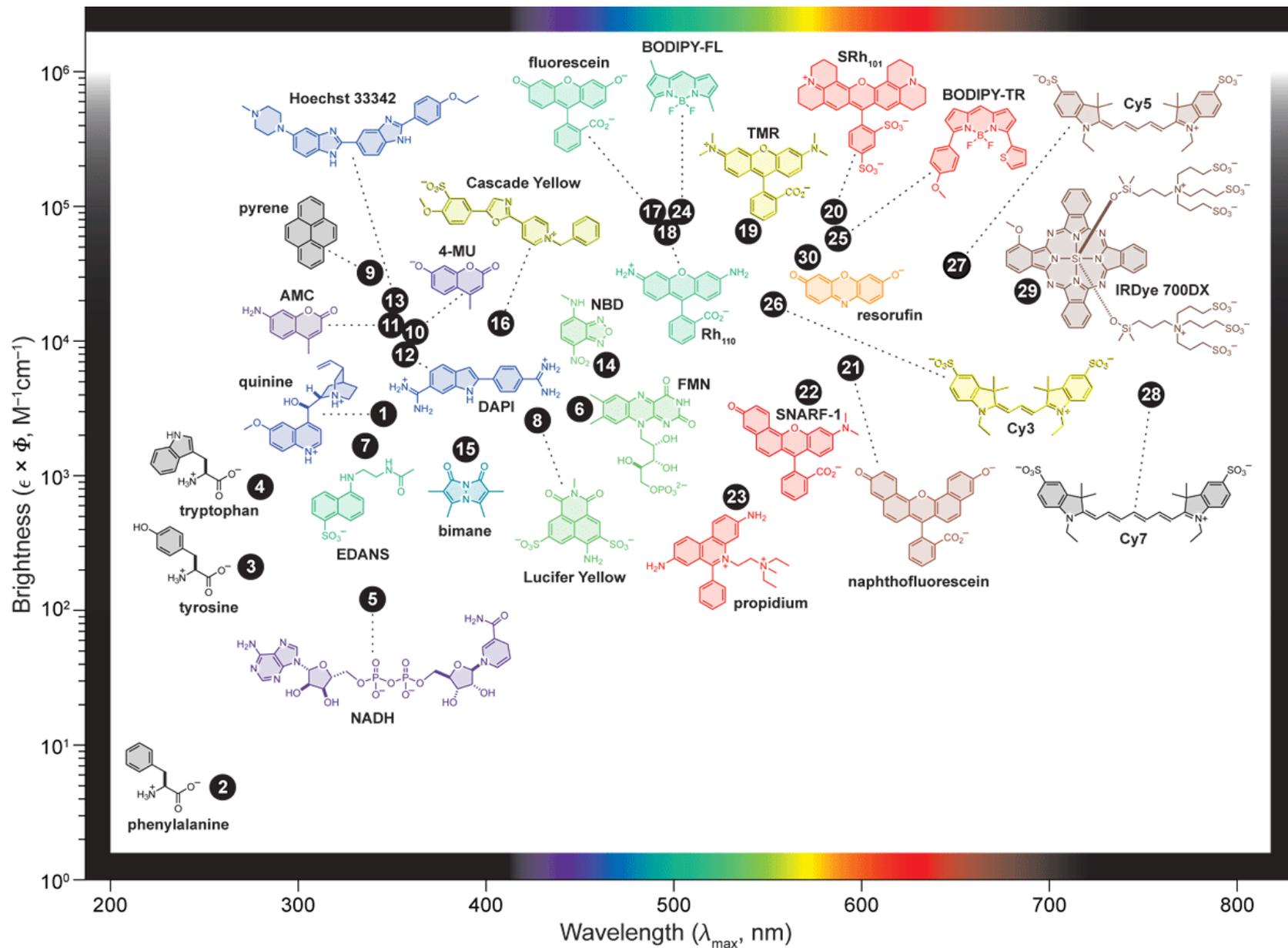


<https://svi.nl/FluorescenceMicroscope>



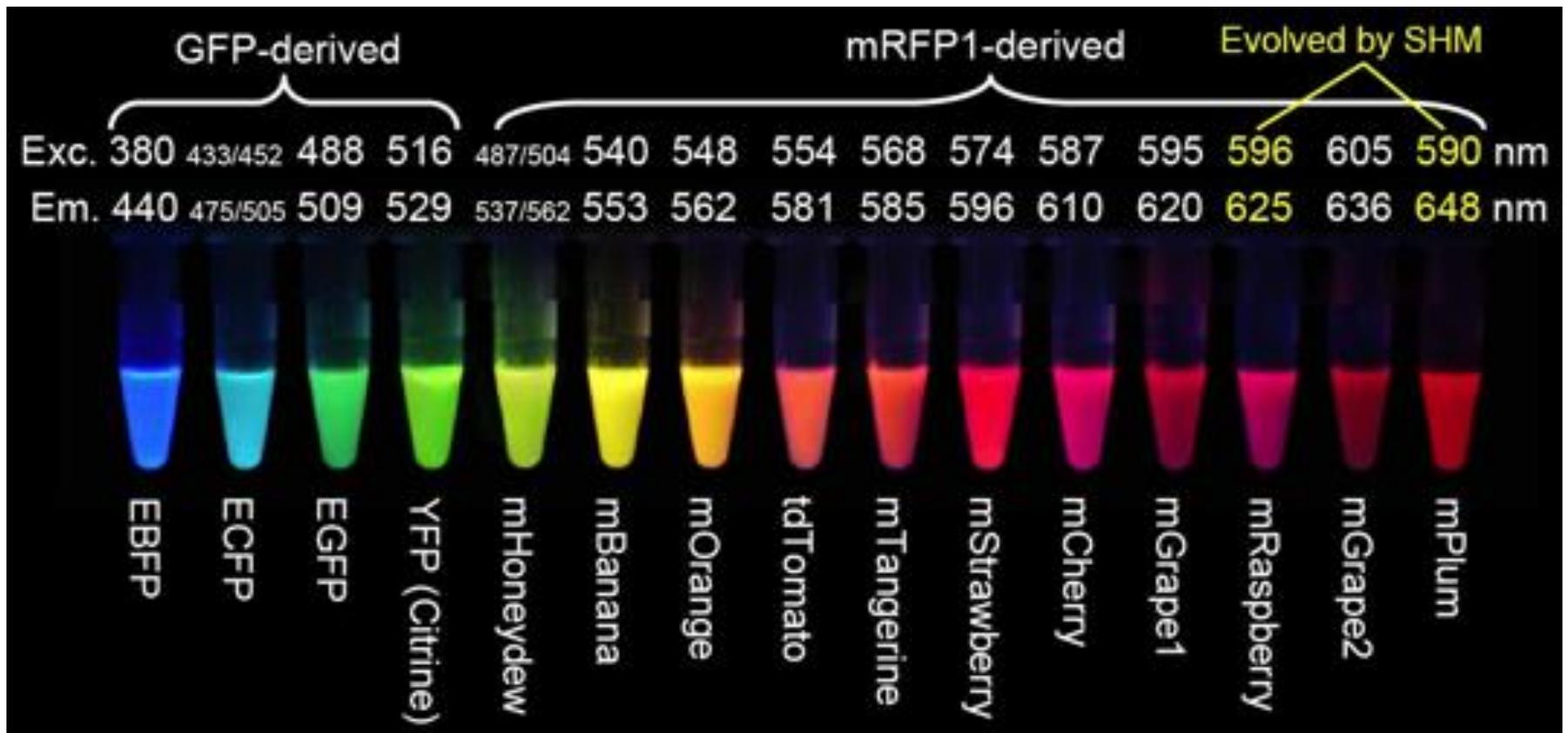
[https://www3.aps.anl.gov/News/APS\\_News/Images/184209-2.gif](https://www3.aps.anl.gov/News/APS_News/Images/184209-2.gif)

# Fluorophores



# Fluorescent Proteins

Derived from naturally-occurring fluorescent proteins in jellyfish, etc.



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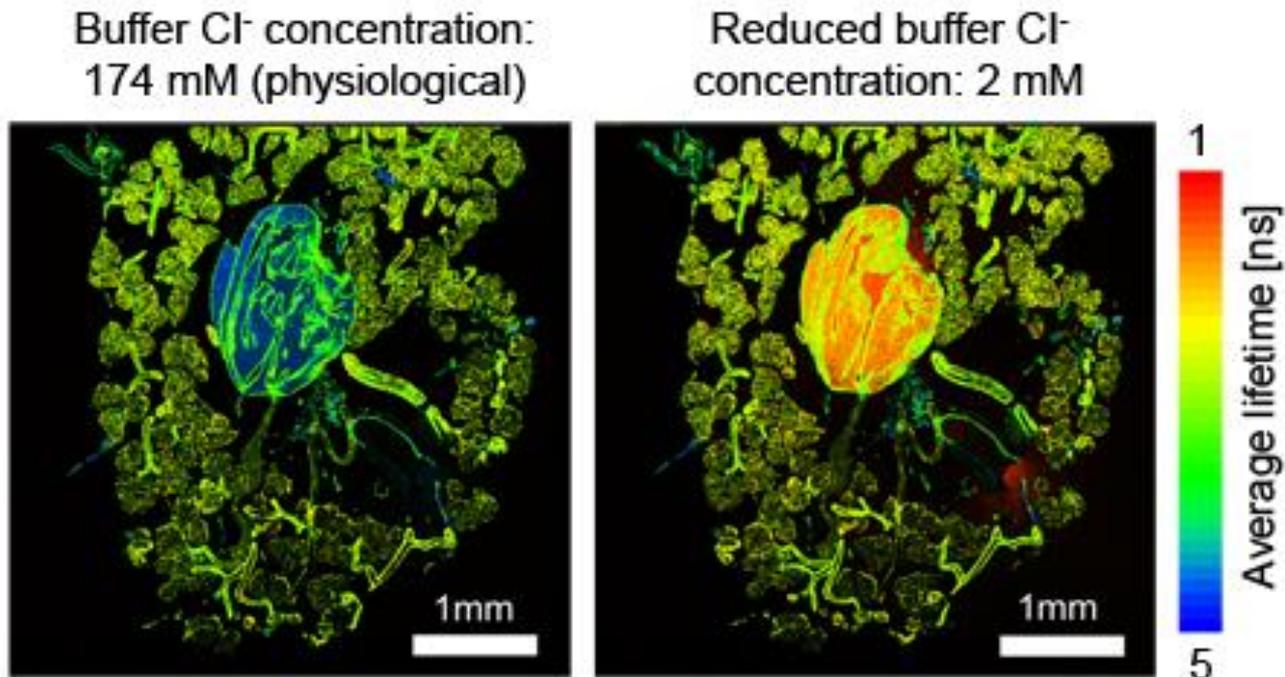
## 3. Fluorescence Imaging techniques

FLIM, FRET, FIONA

## 4. Applications

# Fluorescence-lifetime imaging microscopy (FLIM)

- Spatial imaging by fluorescence lifetime
- Non-intensity based imaging technique



<https://www.picoquant.com/applications/category/life-science/fluorescence-lifetime-imaging-flim#tab-5>

# FLIM in Urbana-Champaign

Robert Clegg – UIUC  
Full-field FLIM



Enrico Gratton – UIUC  
Scanning confocal FLIM



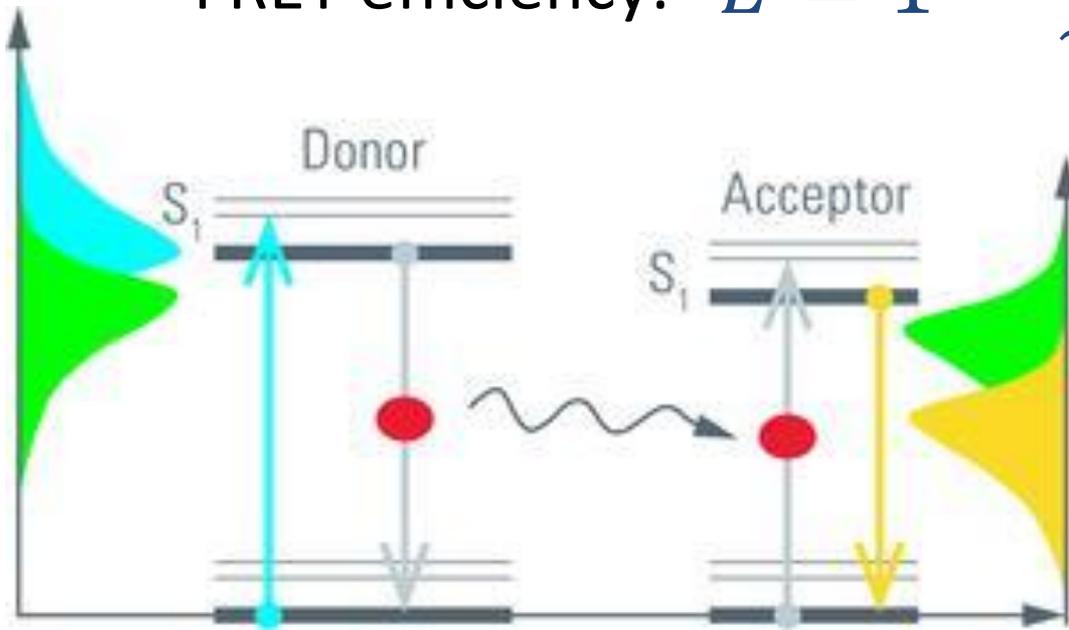
Beniamino Barbieri – ISS Inc.  
Commercialization of FD FLIM



# Förster resonance energy transfer (FRET)

- Donor and acceptor fluorophore attached to different parts of molecule or two bound molecules
- Emission energy of donor matches absorption energy of acceptor

FRET efficiency: 
$$E = 1 - \frac{\tau_{DA}}{\tau_D} = \frac{1}{1 + (r/R_0)^6}$$

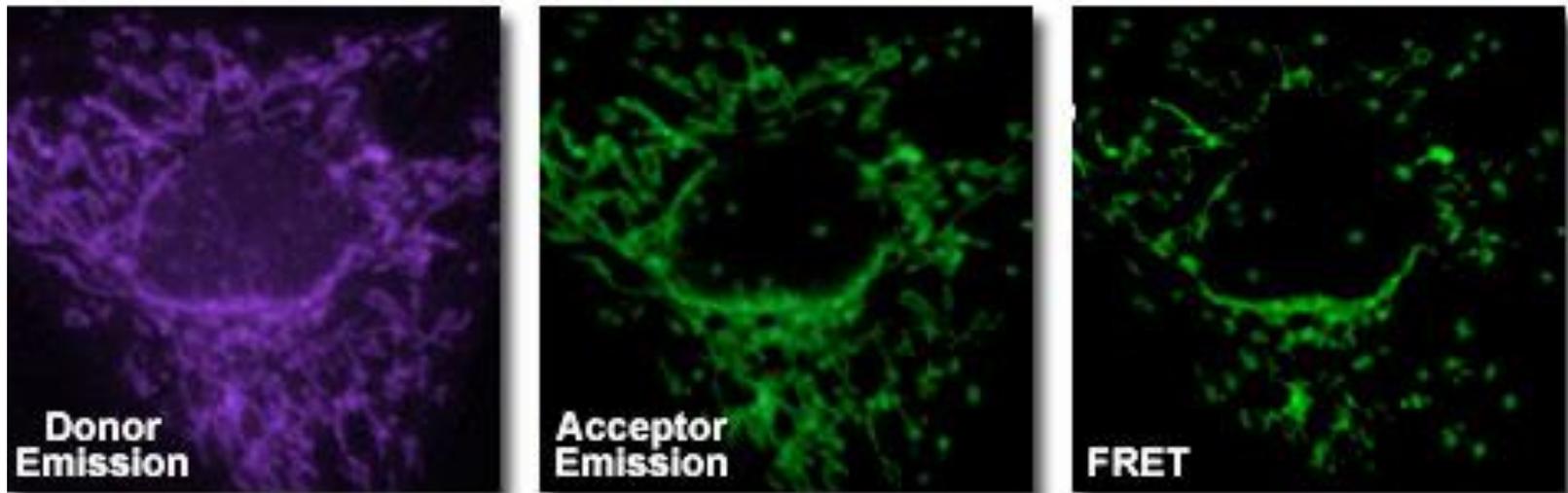


$R_0$ : Förster distance –  
Property of fluorophores

# Ratiometric FRET

$$E_{rel} = \frac{I_A}{I_A + I_D}$$

## Mitochondrial Protein-Protein Association with FRET

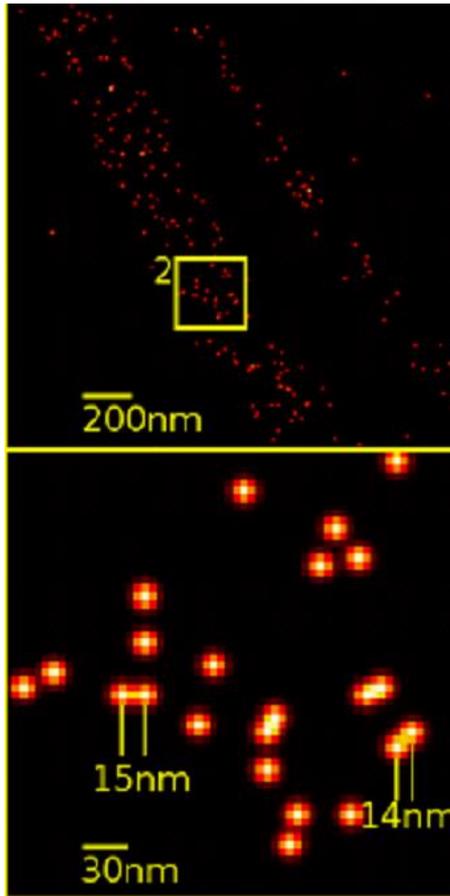


<http://www.olympusmicro.com/primer/techniques/fluorescence/fret/fretintro.html>

$E_{rel} \rightarrow E$  requires correction factors

# Super-resolution microscopy

Optical microscopy limited by diffraction  $d = \frac{\lambda}{2n \sin \theta}$   
 $d_{min} \approx 250 \text{ nm}$

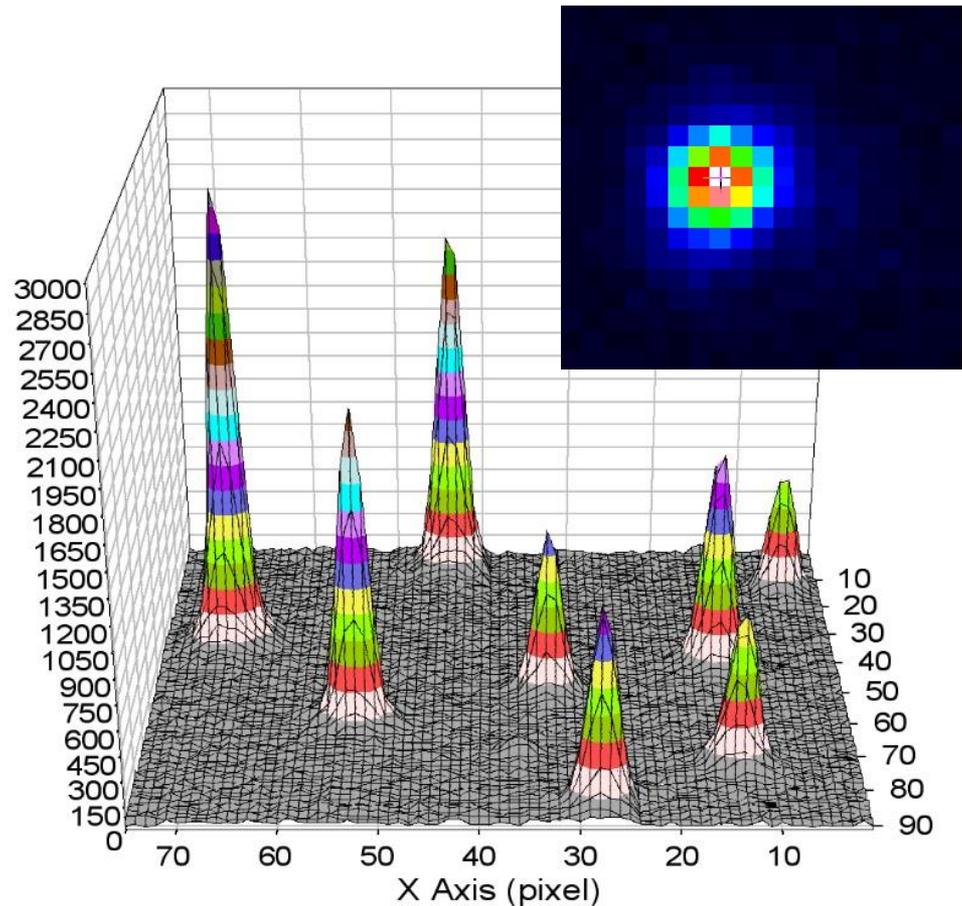


Super-resolution imaging relies on isolating individual fluorophores and fitting the intensity profile to find the center

Can achieve resolution several orders of magnitude finer than diffraction limit

# Fluorescence imaging with one-nanometer accuracy (FIONA)

- Developed by Paul Selvin
- Extreme application of super-resolution imaging
- Requires efforts to maximize signal (use bright fluorophore), and minimize noise (use very sensitive detector)



<https://valelab4.ucsf.edu/external/images/res-singlemolecule/Fig%203a.jpg>

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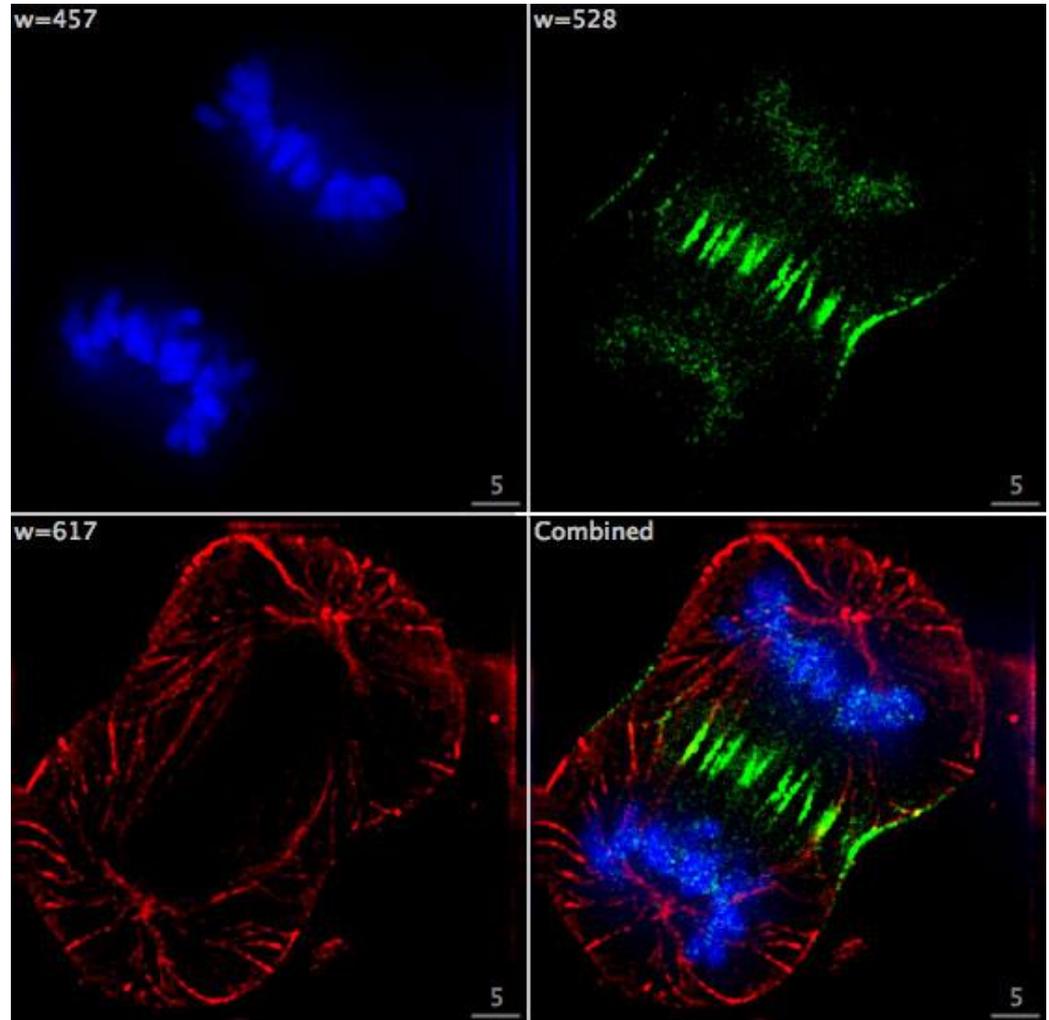
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# Biological applications

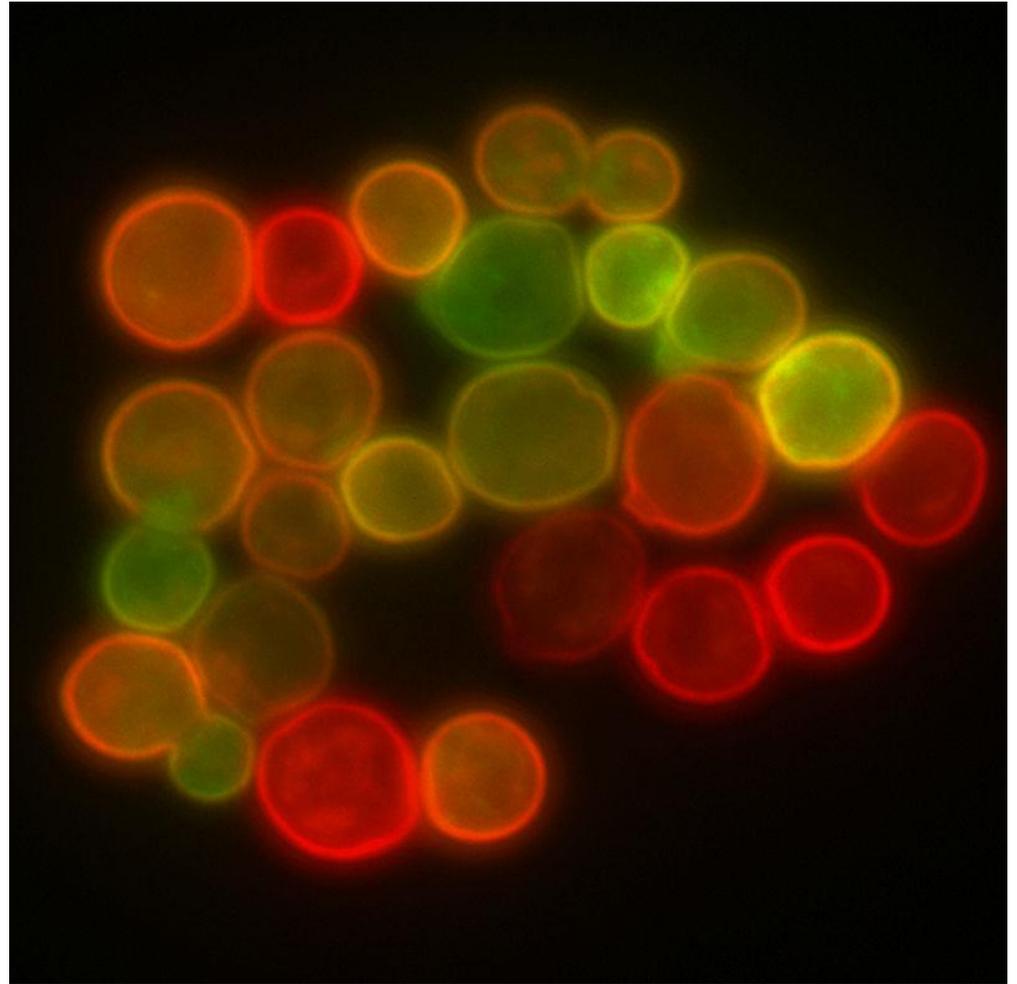
Dividing cancer cell:  
Blue is DNA  
Green is the protein  
INCENP  
Red is microtubules



[https://en.wikipedia.org/wiki/Fluorescence\\_microscope#/media/File:Dividing\\_Cell\\_Fluorescence.jpg](https://en.wikipedia.org/wiki/Fluorescence_microscope#/media/File:Dividing_Cell_Fluorescence.jpg)

# Biological applications

Yeast cell  
membranes labelled  
with red and green  
fluorescent proteins



[https://en.wikipedia.org/wiki/Fluorescence\\_microscope#/media/File:Yeast\\_membrane\\_proteins.jpg](https://en.wikipedia.org/wiki/Fluorescence_microscope#/media/File:Yeast_membrane_proteins.jpg)

# Biological applications

From Thomas Kuhlman

Image of transposon jumping (green) and transposase (red) in E. coli cells



Questions?

